

Exponent rules

$$a^m \cdot a^n = a^{m+n}$$

$$(a^m)^n = a^{mn}$$

$$(ab)^m = a^m \cdot b^m$$

$$\left(\frac{a}{b}\right)^m = \frac{a^m}{b^m} \text{ where } b \neq 0$$

$$a^{-n} = \frac{1}{a^n}$$

$$\frac{1}{b^{-n}} = b^n$$

$$\frac{a^m}{a^n} = a^{m-n}$$

$$\frac{a^{-m}}{b^{-n}} = \frac{b^n}{a^m}$$

$$\left(\frac{a}{b}\right)^{-m} = \left(\frac{b}{a}\right)^m$$

$$\sqrt[n]{a} = a^{\frac{1}{n}}$$

$$\sqrt[n]{a^m} = a^{\frac{m}{n}}$$

$$\sqrt{abc} = \sqrt{a} \cdot \sqrt{b} \cdot \sqrt{c}$$

Exponents

Properties:

$$a^0 = 1 \quad (a \neq 0)$$

$$(ab)^m = a^m b^m$$

$$a^m \cdot a^n = a^{m+n}$$

$$(a^m)^n = a^{mn}$$

$$\frac{a^m}{a^n} = a^{m-n}$$

$$a^{-n} = \frac{1}{a^n}$$

$$\left(\frac{a}{b}\right)^{-n} = \left(\frac{b}{a}\right)^n$$

Examples:

$$10^0 = 1$$

$$(2x)^2 = 2^2 x^2 = 4x^2$$

$$x^2 \cdot x^3 = x^5$$

$$(x \cdot x)(x \cdot x \cdot x) = x^5$$

$$(y^2)^3 = y^6$$

$$(y \cdot y)(y \cdot y)(y \cdot y) = y^6$$

$$\frac{x^5}{x^3} = x^2$$

$$\frac{x \cdot x \cdot x \cdot x \cdot x}{x \cdot x} = x^3$$

$$(6y)^{-2} = \frac{1}{36y^2}$$

$$\text{Note: } 6y^{-2} = \frac{6}{y^2}$$

$$\left(\frac{2x}{3}\right)^{-2} = \left(\frac{3}{2x}\right)^2 = \frac{3^2}{2^2 x^2} = \frac{9}{4x^2}$$